

# Artifactual Functions: A Plan for Analysis

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**Question:** Are these functions instances of a single coherent concept?

**Answer:** Er, um, ... oh look! Isn't that the queen?



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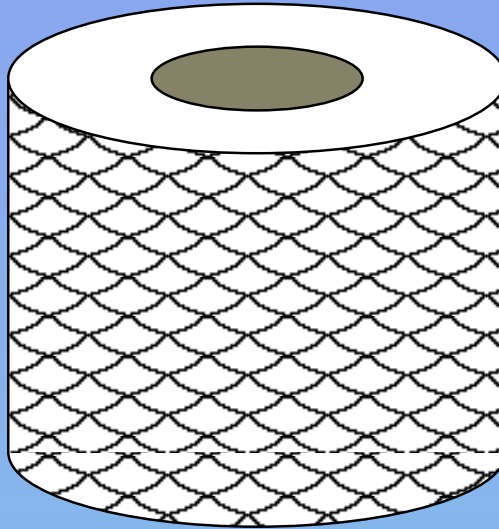
# Artifactual function

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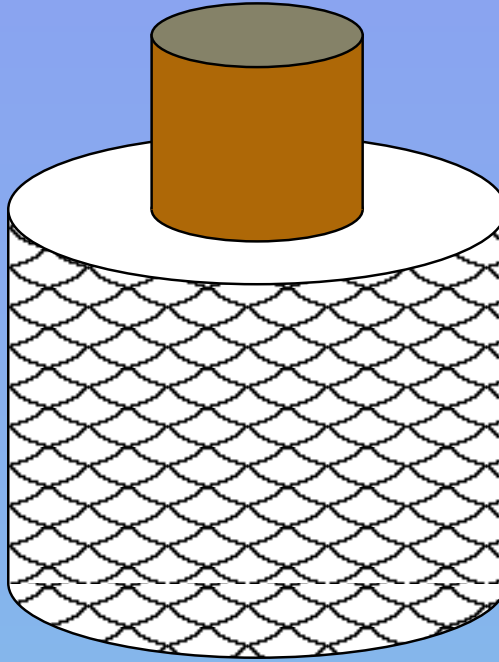
**A very serious example.**



Facial tissue is more expensive than toilet paper.

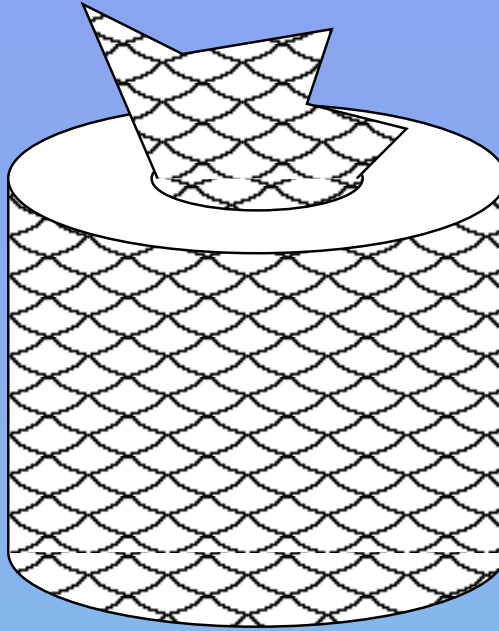


# A very serious example.



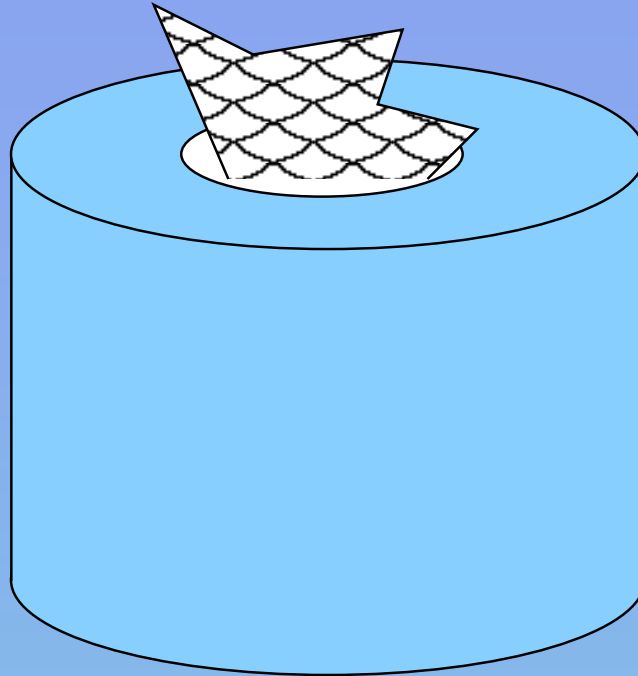
Step one: remove the center piece.

# A very serious example.



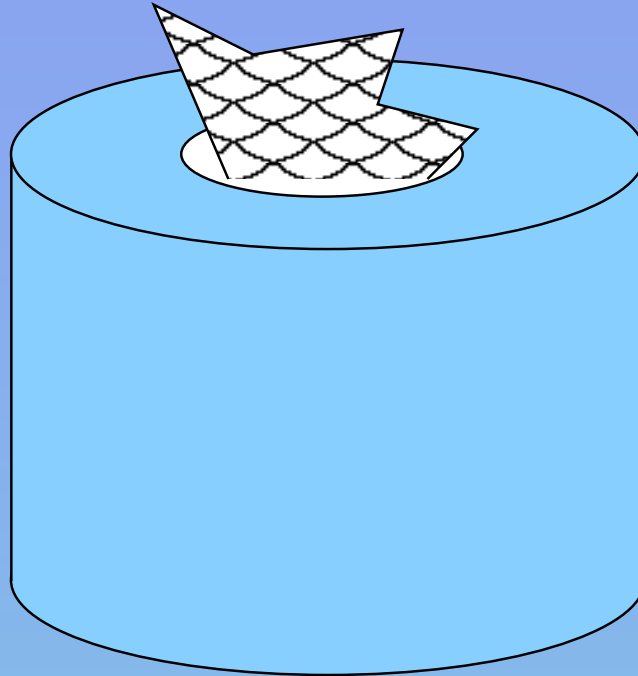
Step two: Dispense tissue via vacant center.

**A very serious example.**



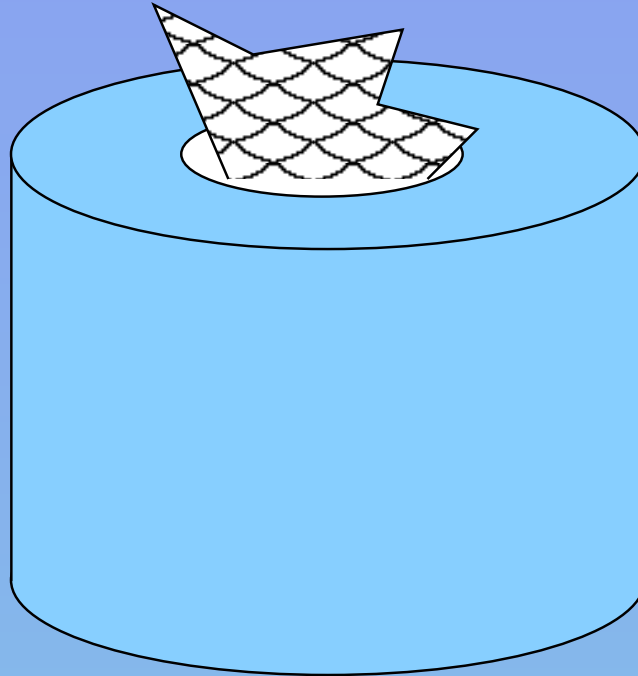
Decorative covers: that Martha Stewart touch.

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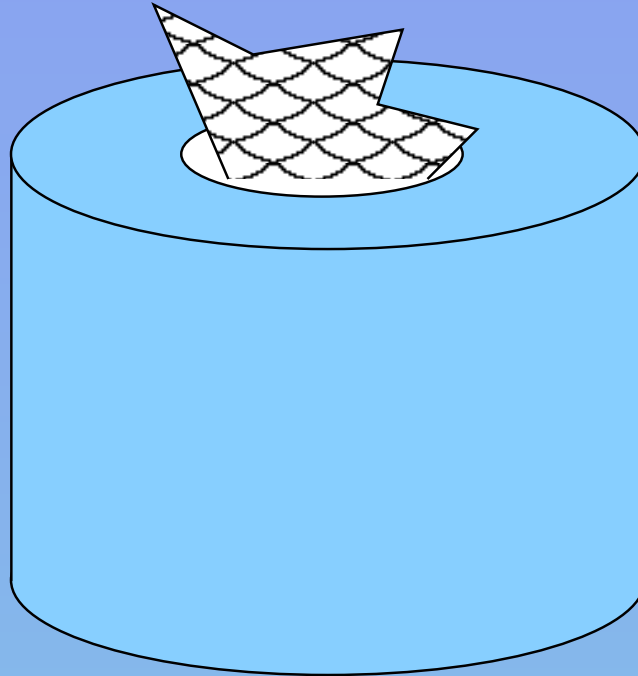
This alternate function arose first as an **accidental** function.

# A very serious example.



It became an example of **repeated use** function (with **designed** accessories).

# A very serious example.



Now coreless rolls of toilet paper are available (i.e.,  
**designed** function).

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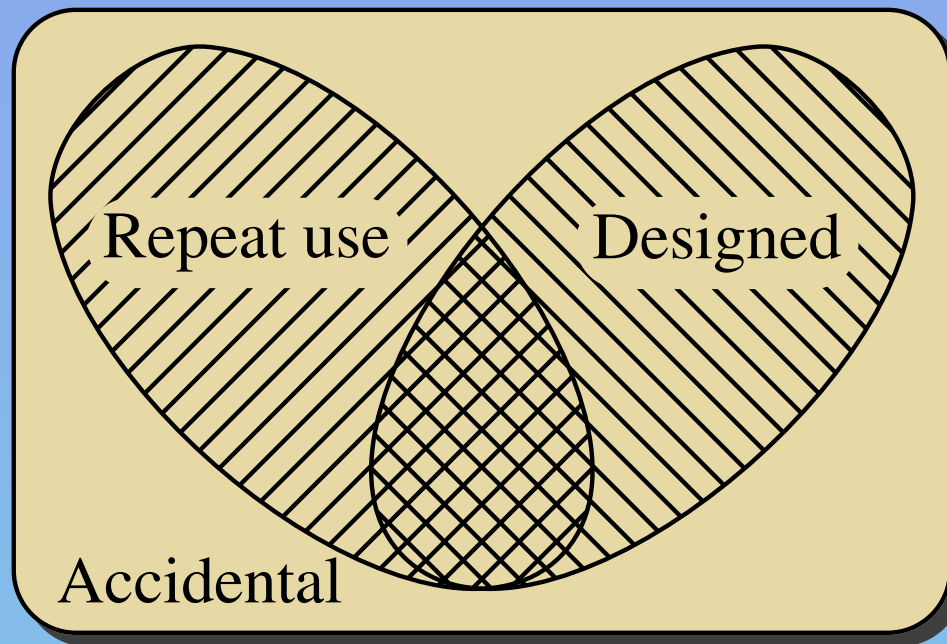


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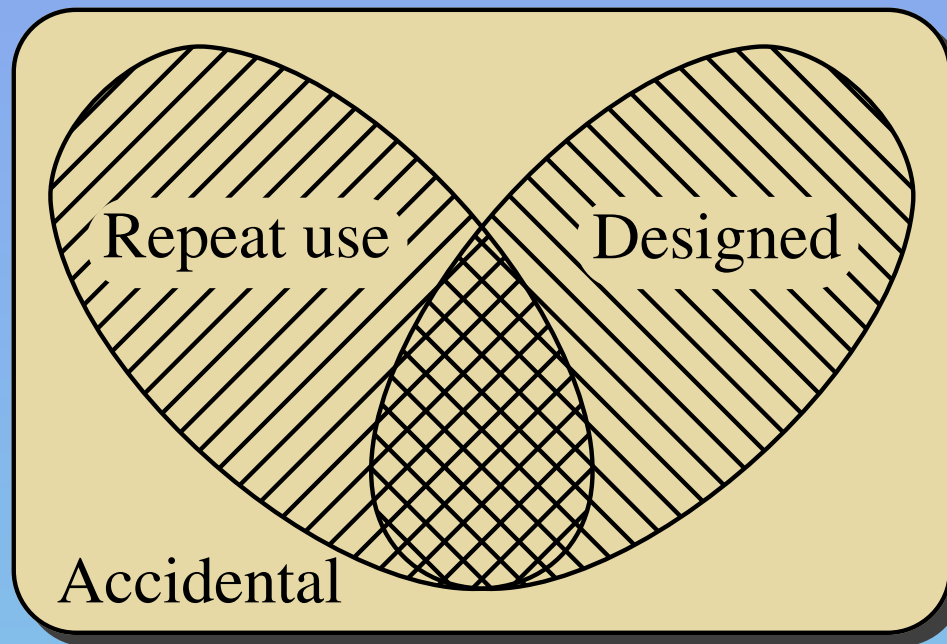


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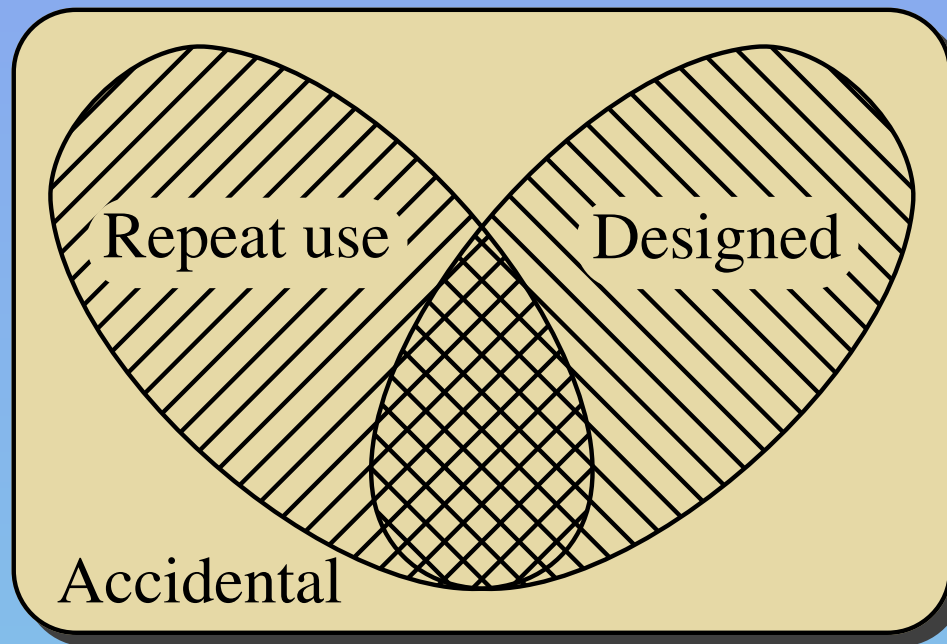
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**(We hope.)**

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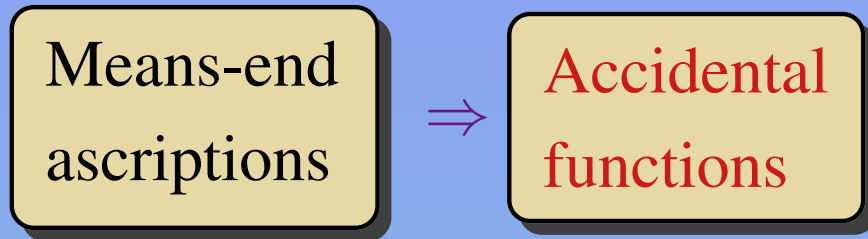
**Procedure: analysis via formalization.**

# The Proposed Development

Means-end  
ascriptions

- Provide formal semantics for means-end ascriptions.

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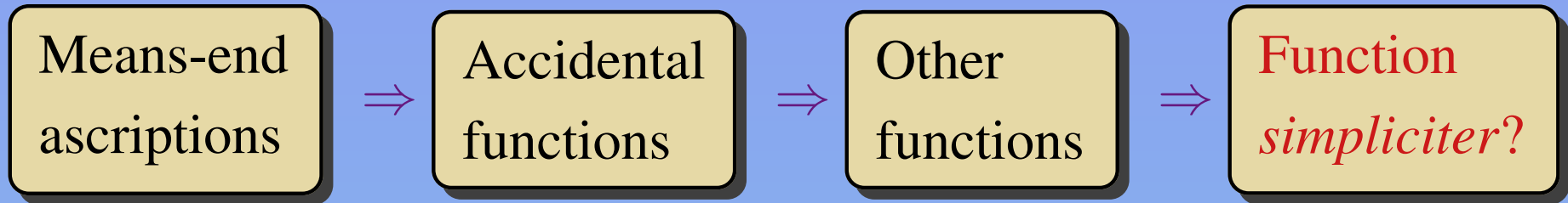
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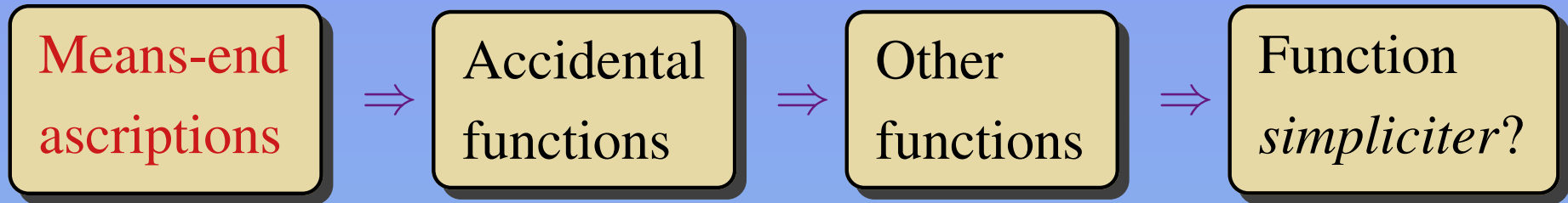
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Today, we restrict our attention to means-end ascriptions.

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**act**

**actions**

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**ME  $\rightarrow$  prop |  $\neg$ ME | ME  $\wedge$  ME | [act] ME**

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But this is a bit too simple...

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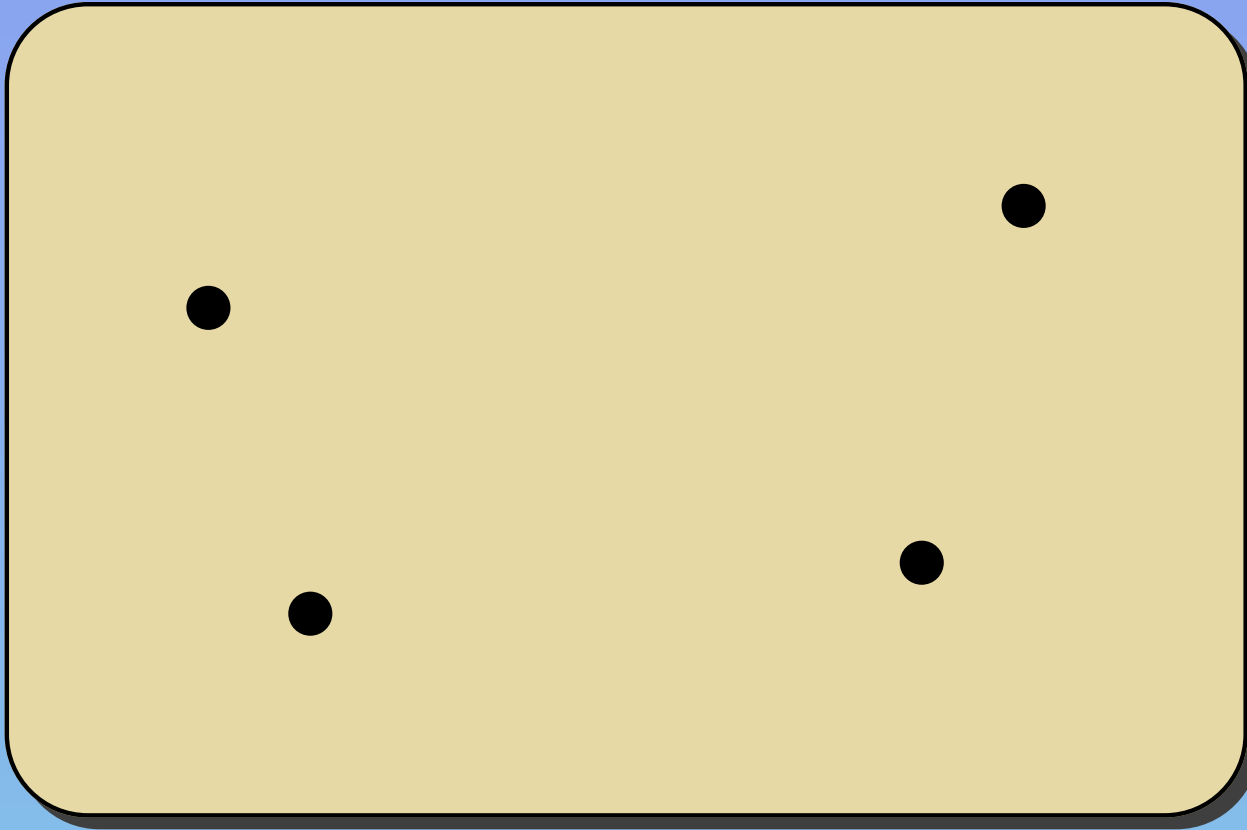
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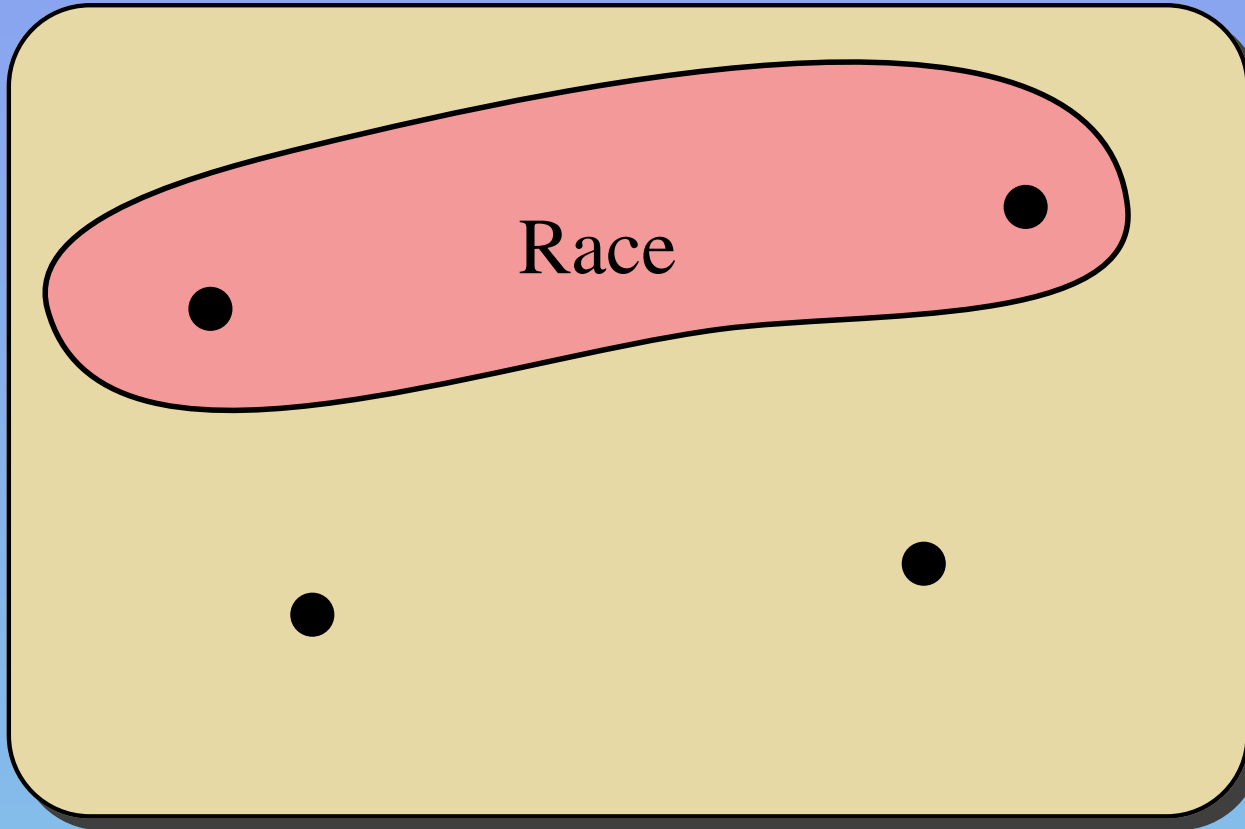
We will ignore  $\Rightarrow$  hereafter.

# Dynamic semantics



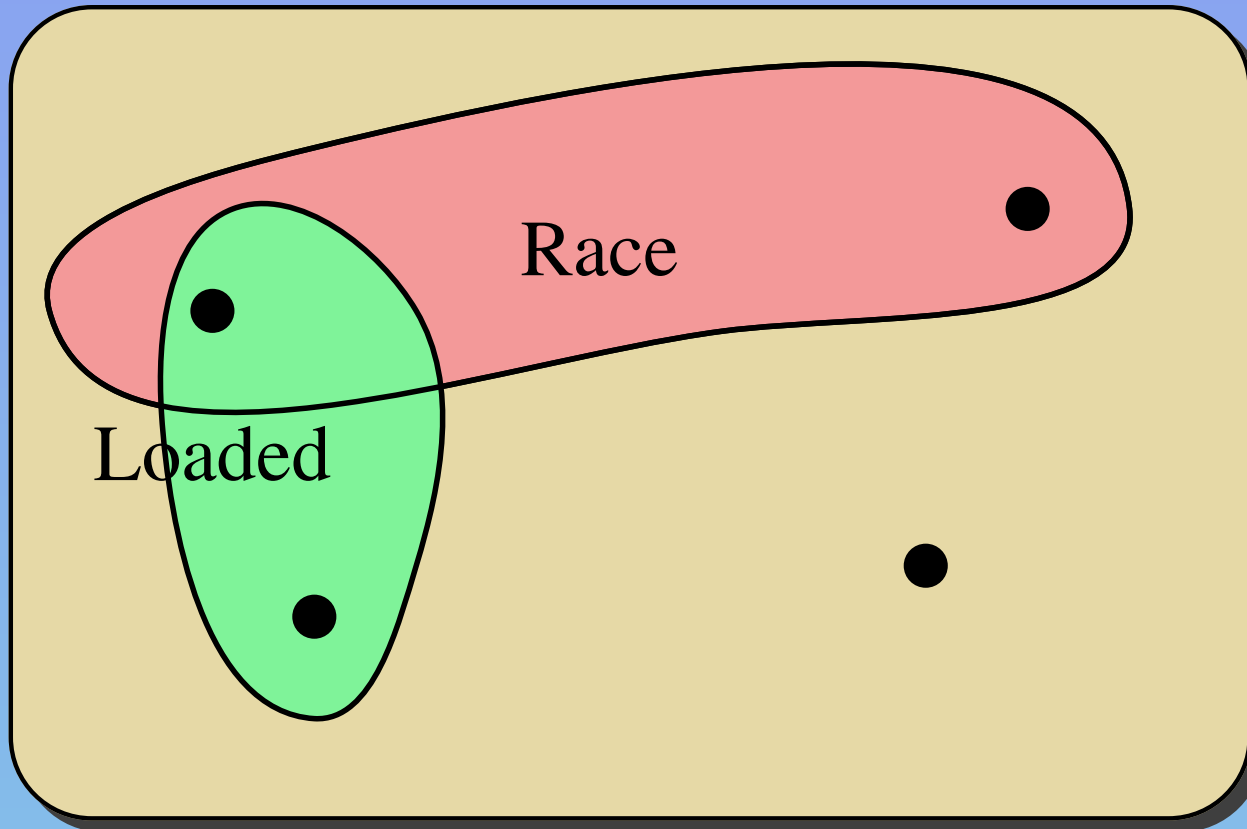
A simple model.

# Dynamic semantics



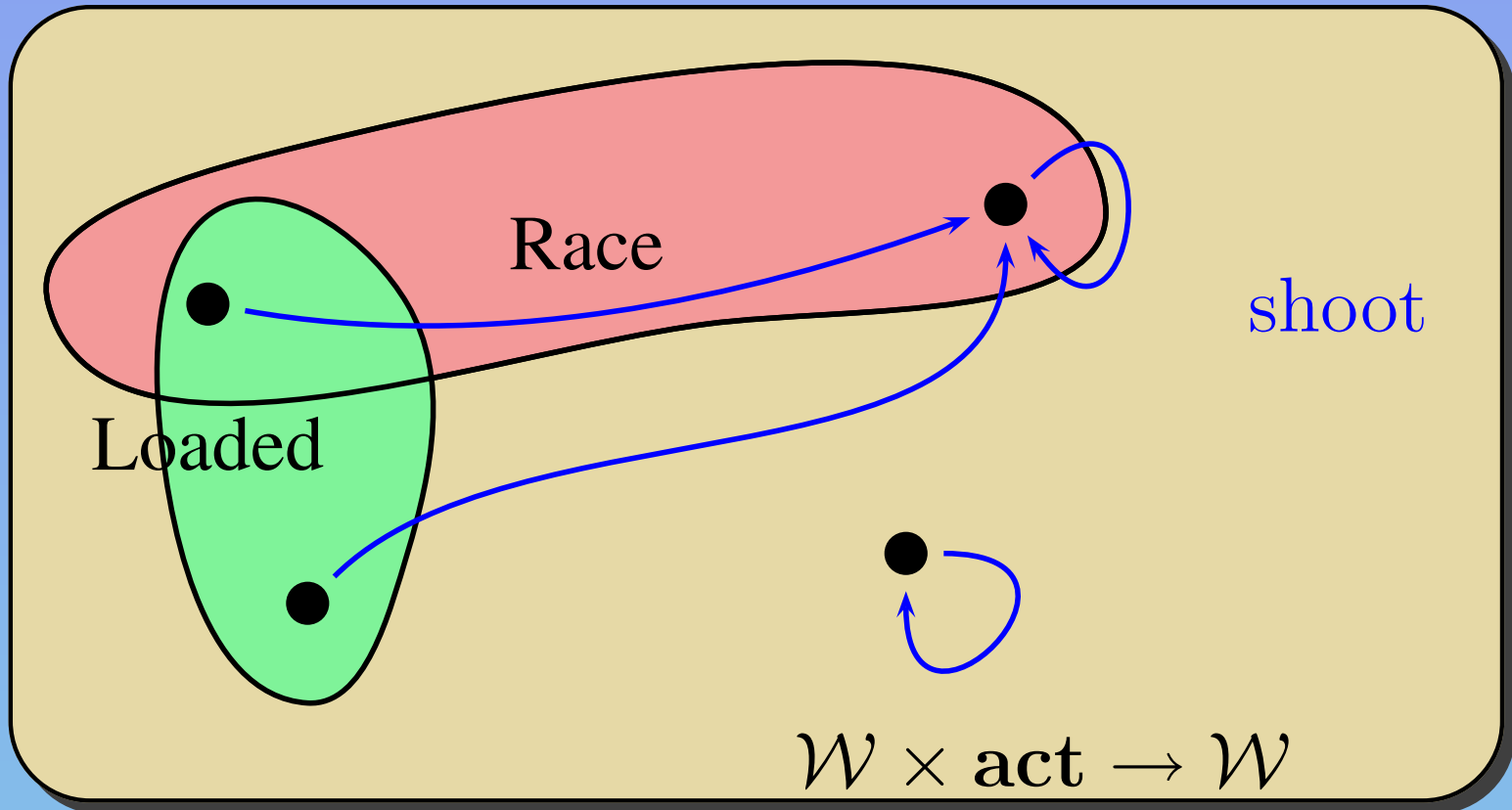
Worlds in which the race has started...

# Dynamic semantics



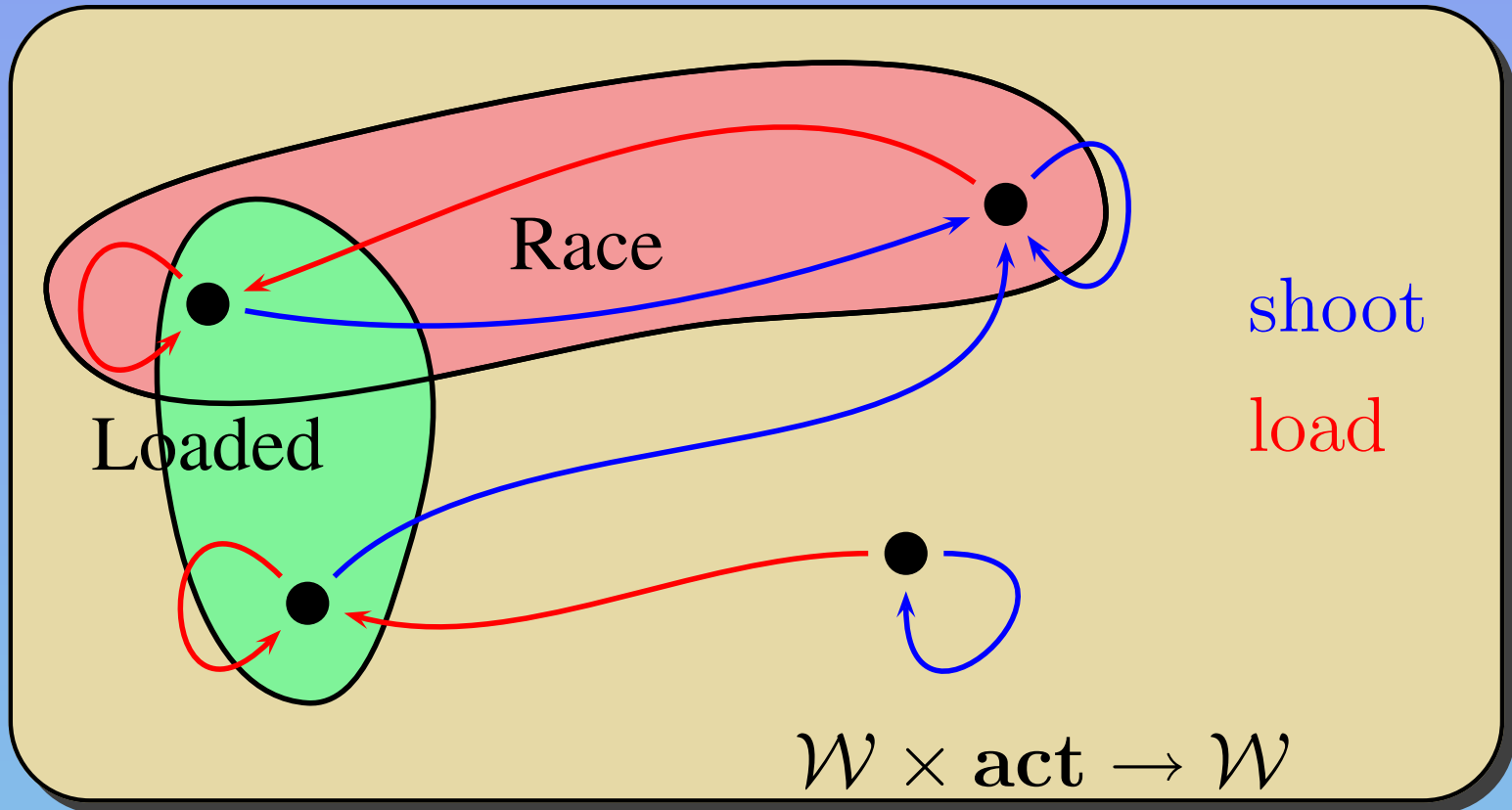
and those in which the gun is loaded.

# Dynamic semantics



The transition structure for shoot...

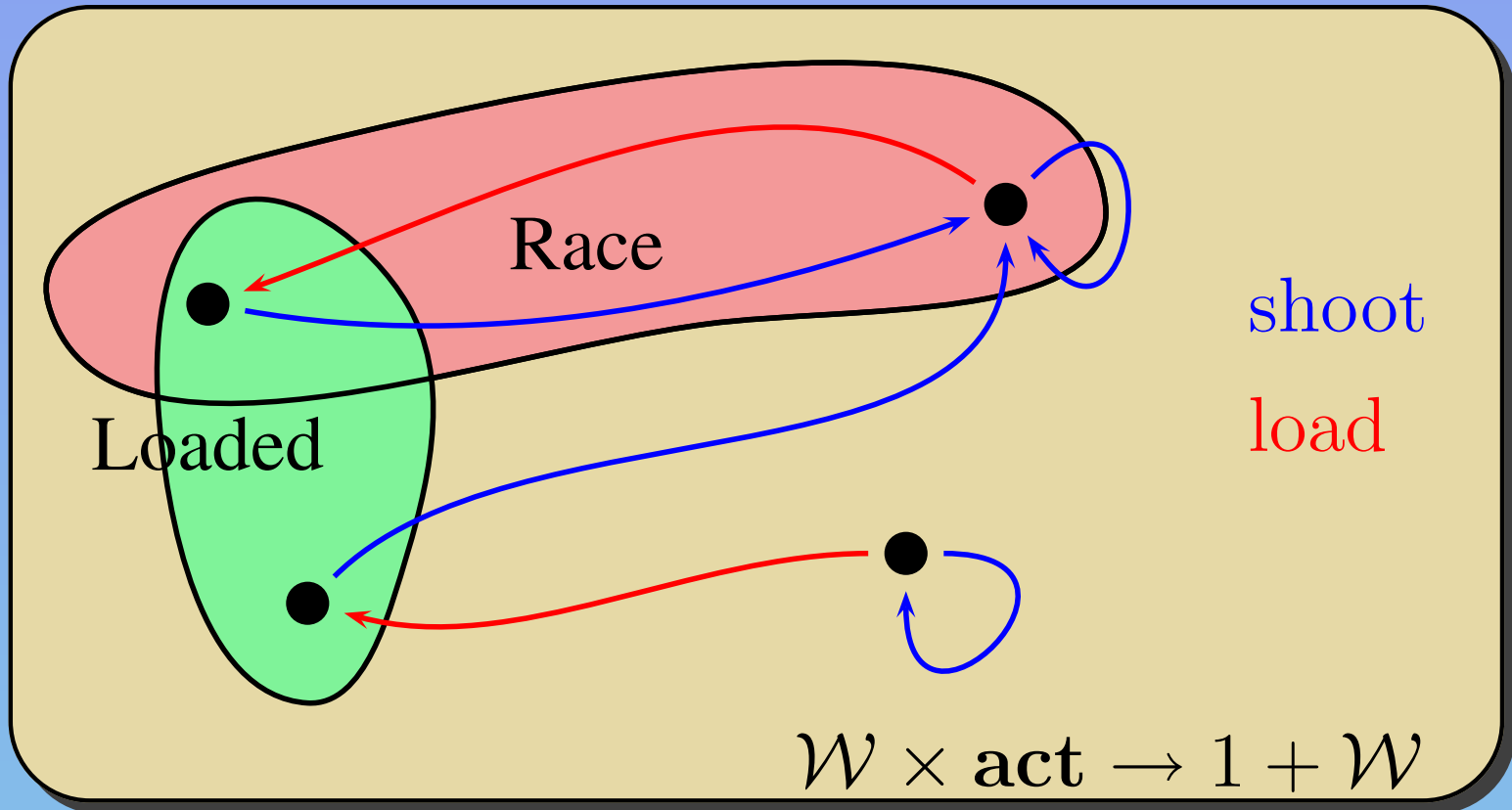
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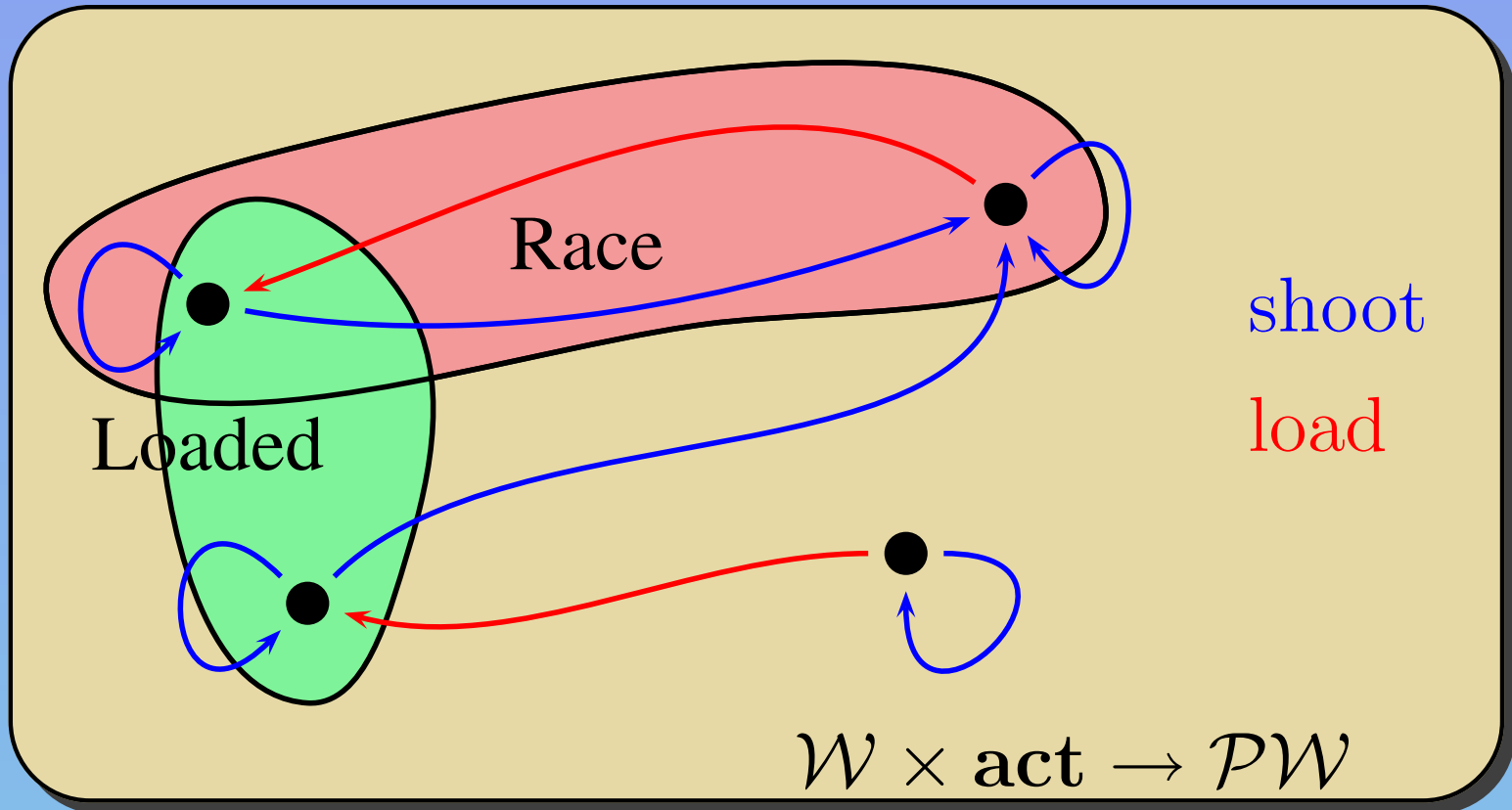


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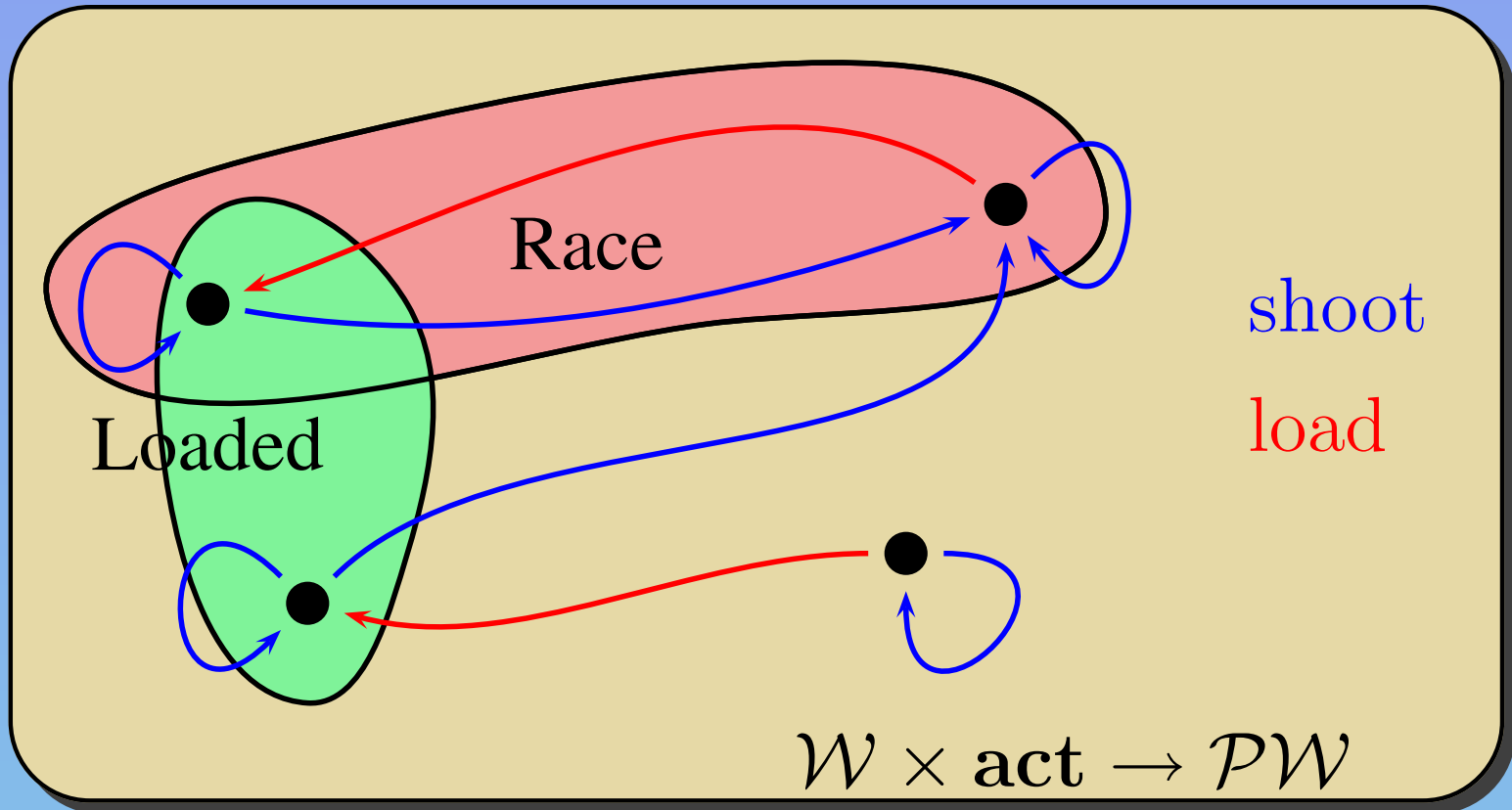
Maybe not every action can be performed in every state.  
(You can't load a loaded gun.)

# Dynamic semantics



Or maybe outcomes are not determined (say, a gun can jam).

# Dynamic semantics



But a jam is less likely than a successful shot. Our semantics should reflect this fact.

# Likelihood semantics

A likelihood model has a transition structure

$$\mathcal{W} \times \text{act} \rightarrow \mathcal{D}(\mathcal{W}),$$

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$$l : \mathcal{W} \times \mathbf{ME} \rightarrow [0, 1].$$

Fixing  $\alpha \in [\frac{1}{2}, 1]$ , we write

$$w \models \varphi \iff l(w, \varphi) \geq \alpha$$

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This is perhaps controversial. Certainly, our likelihood functions are not probability distributions.

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**Distributive semantics:**

$$l(w, [m]\varphi \wedge [m]\psi) = l(w, [m](\varphi \wedge \psi)).$$

# Comparison

*Propositional*

Simple semantics



Distributive semantics



For every purely propositional  $\varphi$ , we have  
 $l(w, \varphi) \in \{0, 1\}$ .

# Comparison

Propositional

Motivation

Simple semantics



Distributive semantics



A simple and compelling argument that the semantics are the right semantics.

# Comparison

Propositional

Motivation

*Modus ponens*

Simple semantics






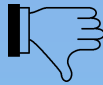
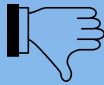



Distributive semantics



If  $w \models \varphi \rightarrow \psi$  and  $w \models \varphi$ , then  $w \models \psi$ .







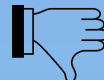



# Comparison

	Propositional	Motivation	Modus ponens	Tautology
Simple semantics				
Distributive semantics				

For every tautology  $\varphi$ , we have  $l(w, \varphi) = 1$ .



# Comparison

	Propositional	Motivation	Modus ponens	Tautology	Equivalence
Simple semantics					
Distributive semantics					

Whenever  $\vdash \varphi \leftrightarrow \psi$ , we have  $l(w, \varphi) = l(w, \psi)$ .

# Concluding remarks

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- Several semantic options for same, including:

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