

A Semantics for Functional Efficacy

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Outline

- 1 Means-end relations and artifactual functions
 - From functions to means-end relations
 - Means-end relations and function fulfillment

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- 2 Efficacy and malfunction
 - Efficacy as a fuzzy property
 - Type-token comparisons and malfunction

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Functional ascriptions



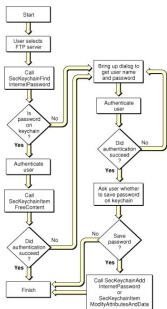
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Functional ascriptions



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- “That switch mutes the television.”

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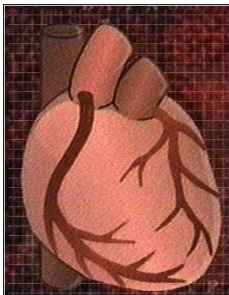
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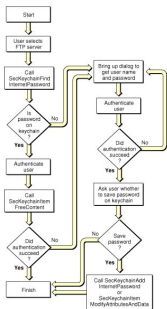
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We focus on artifactual functions.

How functions relate to means and ends



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How functions relate to means and ends



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One can *use* the switch to mute
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- Functions imply means-end relations.

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- Functions imply means-end relations.
- **Aim: Use means-end semantics to analyze functions.**

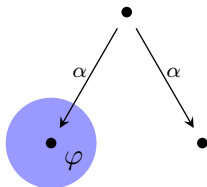
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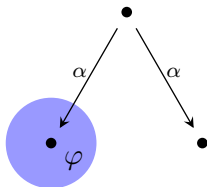


Weak: α might realize φ .

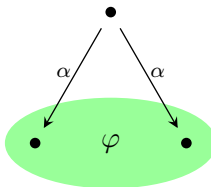
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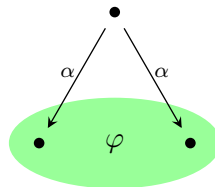
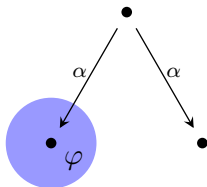


Strong: α *will* realize φ .

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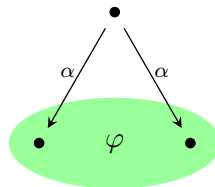
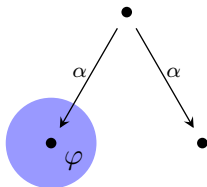
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Both are easily expressed in Propositional Dynamic Logic.

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Result: Formal definitions for “ α is a (weak/strong) means to φ .”

The structure of functional ascriptions

A *functional ascription* f includes the following components.

- an artifact type T ,

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One expects: $\alpha(o, \tau)$ is a means to $\varphi(o, \tau)$.

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Example: fire starters

Various artifacts are used to start fires.

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An *f*-context is given by

- a fire-starting device *o*,
- particular user *u*, weather conditions *c* and kindling *k*.



Token fulfillment

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\Updownarrow
When u ignites k via o in conditions c , kindling k burns.

Functions and subtypes

Subtypes do not always fulfill supertype functions.

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Lighter fulfills *f*, but *CarLighter* does not fulfill *f*.



Type fulfillment

Defined: token fulfills a function f .

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When does a *subtype* $T' \leq T$ fulfill f ?

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every $o \in T'$ fulfills f .

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Normal fulfillment:



every "normal" $o \in T'$ fulfills f .

Normal tokens: the controversial bits

Each type T comes with a set N_T
of *normal* tokens.



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Normal tokens are useful fictions.
Express how T -things are expected to
behave.

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Normal fulfillment:

T fulfills f and $N_{T'} \subseteq N_T \Rightarrow T' \text{ fulfills } f$

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Normal *CarLighters* are not normal *Lighters*.

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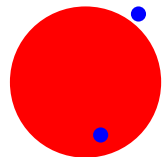
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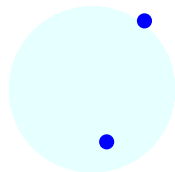
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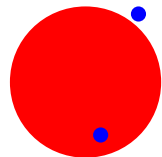
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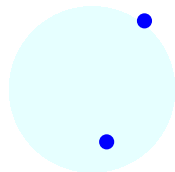
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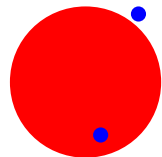
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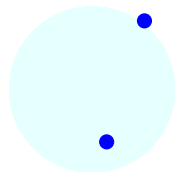
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Efficacy of α in φ :
Truth degree of “ α reliably realizes φ .”



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Fuzzy proposition

Efficacy of artifact types

Token-token comparison:

Can compare efficacy of two tokens.

What about efficacy of an artifact type?

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What is the efficacy of *Lighter* for starting fires?

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f-efficacy of type *T*:

$\text{infimum} \{f\text{-eff. of } o \mid o \text{ is a normal } T\text{-token}\}$



Malfunction as type-token comparison

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A *Lighter* malfunctions when it is ineffective at starting fires.

A *CarLighter* malfunctions when it is less effective than normal *CarLighters*.

Concluding remarks

- Aim: Formal semantics for clarifying natural language.

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Thank you.

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- 3 Function origins
- 4 Extra material on normal tokens

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Start with means-end relations.

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Normal tokens: the excuses

We add fictional objects to our semantics?

What are you thinking?



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- **Distinguishes subtypes.**

